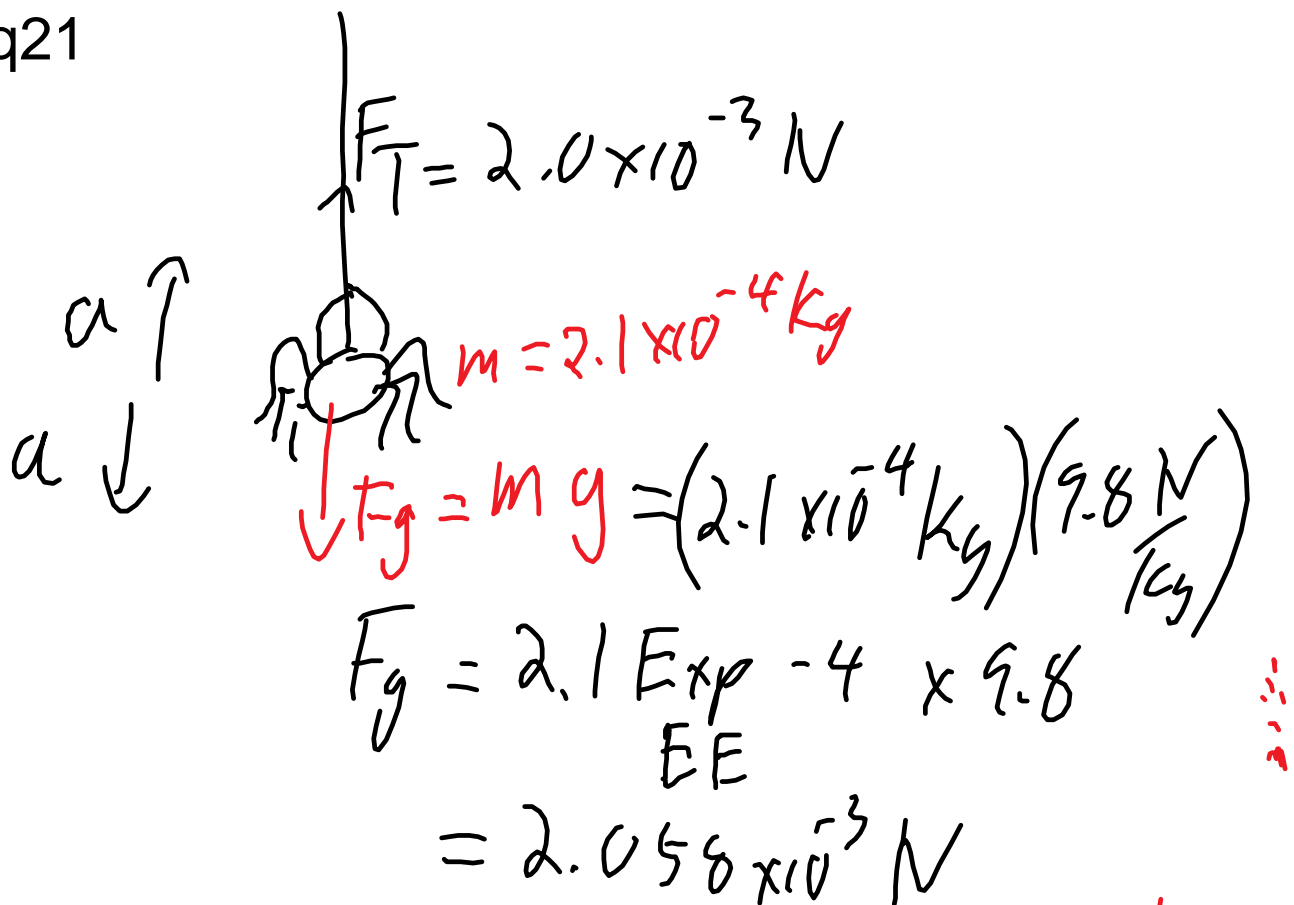


# Review Problems from Chapter 5

p107 q21



A free-body diagram of a mass  $m$ . An upward arrow is labeled  $F_T = 2.0 \times 10^{-3} \text{ N}$ . A downward arrow is labeled  $F_g = m g = (2.1 \times 10^{-4} \text{ kg})(9.8 \frac{\text{N}}{\text{kg}})$ . To the left of the mass, two arrows labeled  $a$  point in opposite directions, one up and one down. Below the diagram, the calculation for  $F_g$  is shown:

$$F_g = 2.1 \times 10^{-4} \times 9.8 = 2.058 \times 10^{-3} \text{ N}$$

$$F_{\text{net}} = ma = \sum F \quad *$$

$$ma = F_g - F_T$$

$$a = \frac{2.058 \times 10^{-3} \text{ N} - 2.0 \times 10^{-3} \text{ N}}{2.1 \times 10^{-4} \text{ kg}}$$

$$a = 0.27619 \text{ m/s}^2$$

$$a = 0.28 \text{ m/s}^2 \text{ down}$$

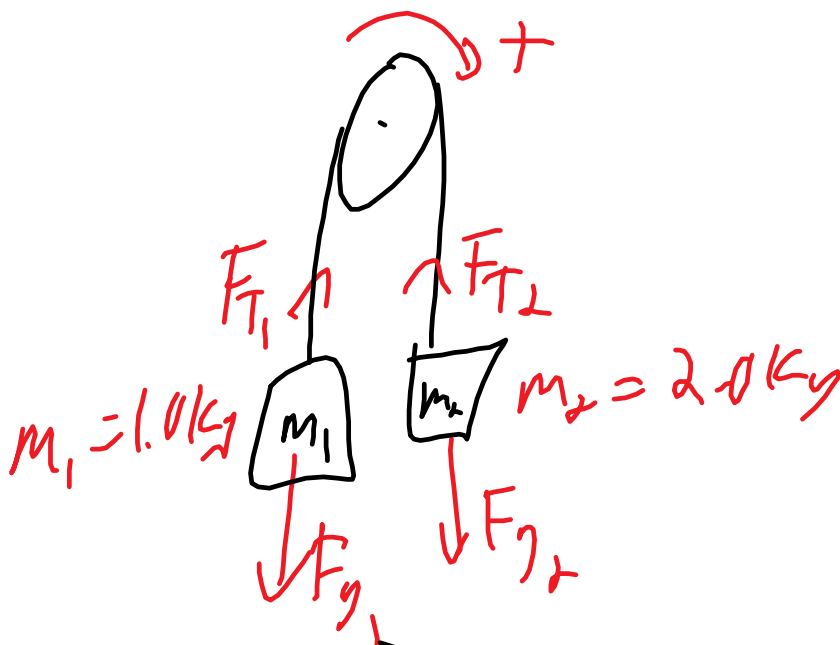


$$ma = (F_T) - F_g$$

$$m = (20 \times 75 \text{ kg}) + 500 \text{ kg}$$

$$2000 \text{ kg } a = 2.96 \times 10^4 \text{ N} - 2000 \text{ kg } (9.8)$$

$$a = 5.0 \text{ m/s}^2 \text{ up}$$



$$F_{net} = (m)a = F_{g2} - F_{g1}$$

$$(m_1 + m_2)a = m_2g - m_1g$$

$$a = \frac{m_2g - m_1g}{m_1 + m_2}$$

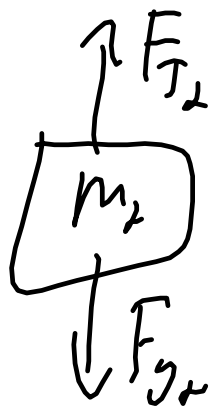
$$a = \frac{2\text{ kg}(9.8\frac{\text{m}}{\text{s}^2}) - 1\text{ kg}(9.8\frac{\text{m}}{\text{s}^2})}{2\text{ kg} + 1\text{ kg}}$$

$$a = 3.2667 \text{ m/s}^2$$

$$a = 3.3 \text{ m/s}^2$$

$m_2$  ↓     $m_1$  ↑

b)



$$\downarrow a = 3.2667 \text{ m/s}^2$$

$$F_{g2} - F_{T2} = m_2a$$

$$F_{g1} - F_{T1} = m_1a$$

$$\begin{aligned}
 F_{T2} &= F_{g2} - m_2 a \\
 &= (2 \text{ kg})(9.8 \frac{\text{m}}{\text{s}^2}) - 2 \text{ kg}(3.267 \frac{\text{m}}{\text{s}^2}) \\
 &= 13.067 \text{ N} \\
 &= \boxed{13 \text{ N}}
 \end{aligned}$$

$\uparrow F_{T1}$   
 $\boxed{m_1}$   
 $\downarrow F_{g1}$

$\uparrow a$

$$m_1 a = F_{T1} - F_{g1}$$

$$F_{T1} = F_{g1} + m_1 a$$

$$\begin{aligned}
 F_{T1} &= (1 \text{ kg})(9.8 \frac{\text{m}}{\text{s}^2}) + 1 \text{ kg}(3.267) \\
 &= 9.8 + 3.267 \\
 &= 13.067 \text{ N} \\
 &= \boxed{13 \text{ N}} \text{ Same!}
 \end{aligned}$$

# Momentum and Impulse (chapter 9)

not on the test next class

## Review

What is inertia?

The tendency of an object to not accelerate.  
objects at rest tend to stay at rest, objects in motion tend to stay in straight line constant speed motion.

Things with more mass have more linear inertia.

Momentum - inertia in motion

symbol is  $p$  (why, I don't know - pneumatics?)

define as the product of mass and velocity

$$p = mv$$

units:  $\text{kgm/s}$

momentum is a vector - has direction - same direction as the velocity

What happens if you apply unbalanced force to a mass,  $m$ ?

$F_{\text{net}} = ma$  acceleration  $a = \Delta v / \Delta t$

$F_{\text{net}} = m \Delta v / \Delta t$  if the mass is constant then

$$m \Delta v = \Delta p$$

and

$F_{\text{net}} = \Delta p / \Delta t$  slope of the  $p$ - $t$  graph is  $F_{\text{net}}$

$$\Delta p = F_{\text{net}} \Delta t$$

We call this quantity, impulse  
=  $\Delta p$  or  $F_{\text{net}} \Delta t$  or area under the  $F_{\text{net}} - t$  graph

eg.

You throw a 0.145 kg baseball at  
60 miles/hour (1.6km/mile)(1000m/km)  
(1hour/3600s)

$$60 \times 1.6 \times 1000 / 3600 = 26.6667 = 26.67 \text{ m/s.}$$

The batter hits the baseball and it goes back  
at -40.0 m/s. If the ball is in contact with the bat  
for 0.020s, what is the

- momentum of the ball before and after being hit?
- Impulse on the ball? Impulse on the bat?
- Average force on the ball and bat while in contact?
- keepers - sketch a graph of the force over time given it increases and decreases linearly.

study for the test  
p178 Q1-4

$$\begin{aligned} \text{a) } p &= mv = 0.145 \text{ kg} \times 26.67 \text{ m/s} = 3.87 \text{ kgm/s before} \\ &= 0.145 \text{ kg} \times -40 \text{ m/s} \\ &= -5.8 \text{ kgm/s} \end{aligned}$$

$$\begin{aligned} \text{b) impulse} &= \Delta p = F_{\text{net}} \Delta t \\ &= p_f - p_i = -5.8 \text{ kgm/s} - 3.87 \text{ kgm/s} \end{aligned}$$

-5.8-3.87=-9.67 kgm/s on the ball  
 impulse on the bat is equal and opposite  
 9.67 kgm/s

c)  $\Delta p = F_{\text{net}} \Delta t$

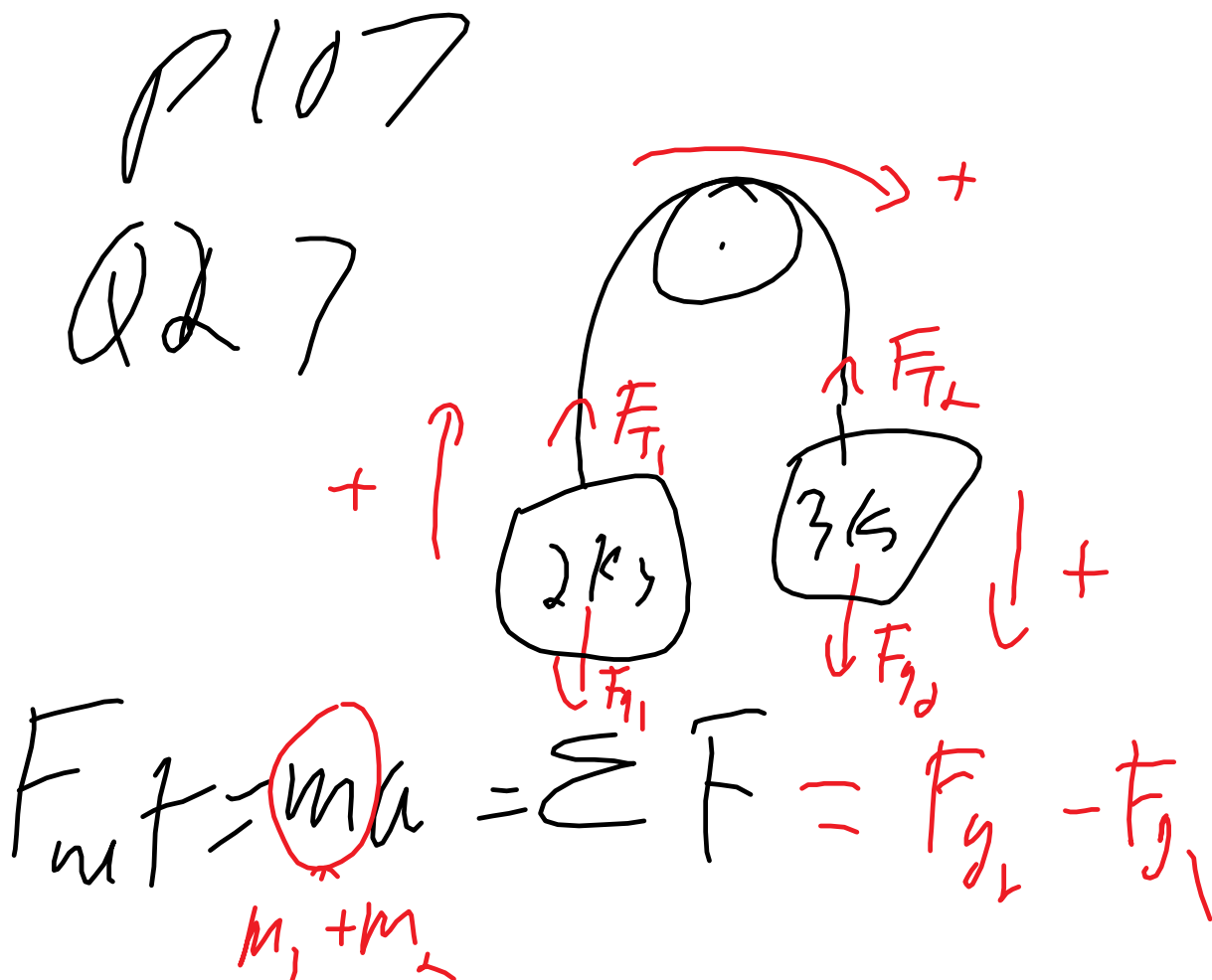
$F_{\text{net}} = \Delta p / \Delta t = -9.67 \text{ kgm/s} / 0.020 \text{ s}$

$9.67 / 0.02 = 483.5$

-4.8 x 10<sup>2</sup> N on the ball

+4.8 x 10<sup>2</sup> N on the bat

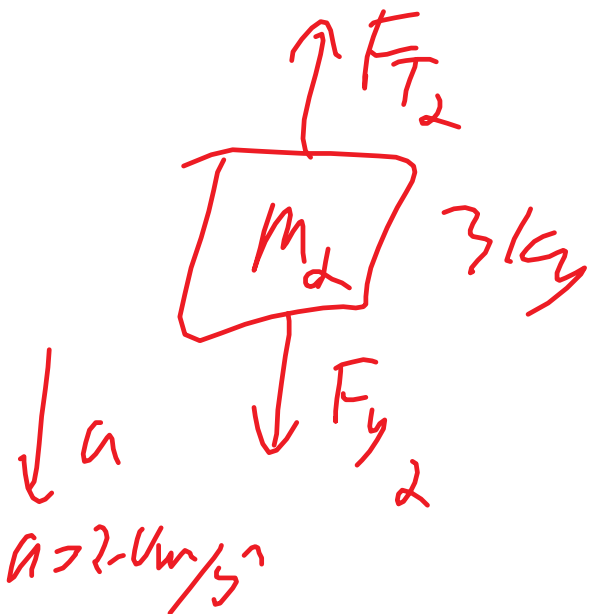
d) keepers do this at home  
 everyone study for the test



$$(m_1 + m_2)a = m_2g - m_1g$$

$$a = \frac{3\text{kg}(9.8 \frac{\text{m}}{\text{s}^2}) - 2\text{kg}(9.8 \frac{\text{m}}{\text{s}^2})}{2\text{kg} + 3\text{kg}}$$

$$a = 2.0 \text{ m/s}^2$$



$$ma = F_{g2} - F_{T2}$$

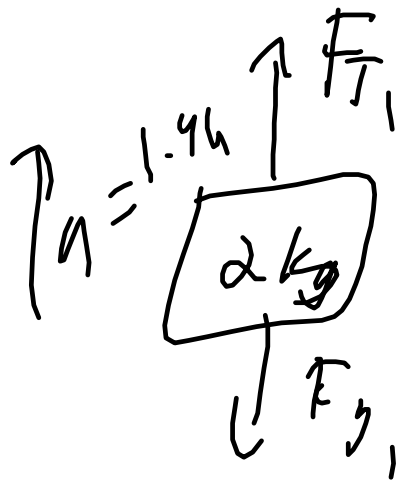
$$(3\text{kg})(2.0 \text{ m/s}^2) = 3\text{kg}(9.8) - F_T$$

$$F_T = 23.52 \text{ N}$$

$$F_T = 24 \text{ N}$$

$$\uparrow F_T$$





$$m_1 a = F_{T1} - F_{g1}$$

$$F_{T1} = m_1 a + m_1 g$$

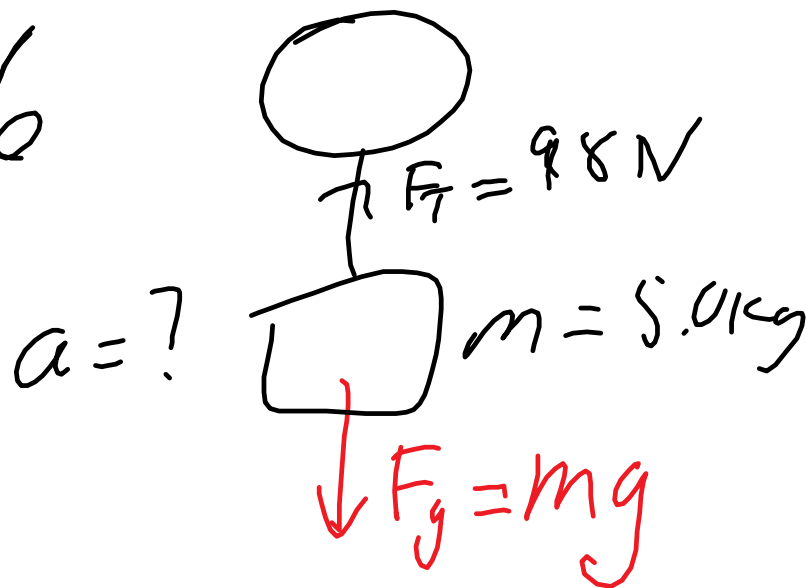
$$F_{T1} = 2 \text{ kg} (1.96 \text{ m/s}^2) + 2 \text{ kg} (9.8 \frac{\text{N}}{\text{kg}})$$

$$= 27.52 \text{ N}$$

$$= \boxed{24 \text{ N}}$$

Same !!!

Q26



$$m a = \sum F = F_T - m g$$

$$a = \underline{98 \text{ N} - (5 \text{ kg})(9.8 \text{ N/kg})}$$

$$a = \frac{10 \text{ N} - (5 \text{ kg})(9.8 \text{ m/s}^2)}{5 \text{ kg}}$$

$$\underline{a = 9.8 \text{ m/s}^2 \text{ up}}$$

b)  $t = 10 \text{ s}$  then  $F_t \rightarrow 0$

$$V_f = 9.8 \text{ m/s}^2 (10 \text{ s}) = 98 \text{ m/s} \text{ up}$$

c)  $F_{\text{net}} = F_g$  since  $F_t = 0$

$$= \boxed{49 \text{ N}}$$

d)  $V_f = v_i + at$

$$0 = 98 \text{ m/s}^2 + (-9.8 \text{ m/s}^2)t$$

$$\boxed{t = 10 \text{ s}}$$

Q 22

$$\boxed{5 \text{ kg}},$$

a)  $F_g$

b)  $F_a$  start

$$(5 \text{ kg})$$

$$\mu_s = 0.30$$

$$\mu_k = 0.10$$

b)  $F_a$  start

c)  $F_a$   $v$  constant

d)  $a = 3.0 \text{ m/s}^2$   
 $F_a = ?$

$$a) F_g = mg = 50 \text{ kg} (9.8 \frac{\text{N}}{\text{kg}})$$

$$= \boxed{490 \text{ N}}$$

$$b) F_a = F_f \quad \text{if } a = 0$$

$$F = \mu_s F_N = 0.30 (490 \text{ N})$$

$$F_a = 147 \text{ N}$$

$$c) F = \mu_k F_N = \underline{0.1} (490 \text{ N})$$

$$\boxed{F_a = 49 \text{ N}}$$

$$d) \begin{array}{c} \leftarrow F_a \quad \boxed{\phantom{000}} \quad \rightarrow F_g \\ \phantom{\leftarrow} \phantom{\rightarrow} \end{array} \quad F_a - F_f = ma$$

$$F_g = ma + F_L$$

$$F_a = 50(3\text{ m/s}^2) + 49\text{ N}$$

$$F_a = 199\text{ N}$$

Momentum and Impulse (chapter 9)  
not on the test next class

Reminder:

Inertia - objects at rest tend to stay at rest,  
objects in motion tend to stay in constant  
speed, linear motion unless a force acts on it.

momentum - inertia with motion

define : the product of mass and velocity

symbol: p (pneumatics greek for forces?)

$$p = mv$$

units: kgm/s

vector quantity - has direction - same as the  
velocity

Impulse - a change in momentum

$$\Delta p = ?$$

$$\Delta p = ?$$

!

motion is changed by a net force

$$F_{\text{net}} = ma \quad a = \Delta v / \Delta t$$

$$F_{\text{net}} = m \Delta v / \Delta t$$

if  $m$  is constant then

$$F_{\text{net}} = \Delta p / \Delta t \quad \text{or the slope of a } p\text{-}t \text{ graph}$$

$$\Delta p = F_{\text{net}} \Delta t \quad \text{or the area under a } F_{\text{net}} - t \text{ graph}$$

eg.